



# **Algebra I Learning Acceleration Guidance**

Learning acceleration will ensure students have the skills they need to equitably access and practice on-grade level content. This chart is a reference guide for teachers to help them more quickly identify the specific prerequisite and co-requisite standards necessary for every Algebra I standard. Students should spend the large majority of their time on the major work of the grade ( $\blacksquare$ ). Supporting work ( $\blacksquare$ ) and, where appropriate, additional work ( $\blacksquare$ ) can engage students in the major work of the grade.

| Algebra I Standard                              | Previous Grade(s) Standards                   | Algebra I Standards Taught in Advance | Algebra I Standards Taught Concurrently |
|---|---|---------------------------------------|---|
| A1: N-RN.B.3                                    | 8.NS.A.1                                      |                                       |   |
| Explain why the sum or product of two           | Know that numbers that are not rational are   |                                       |   |
| rational numbers is rational; that the sum of a | called irrational. Understand informally that |                                       |   |
| rational number and an irrational number is     | every number has a decimal expansion; for     |                                       |   |
| irrational; and that the product of a nonzero   | rational numbers show that the decimal        |                                       |   |
| rational number and an irrational number is     | expansion repeats eventually. Convert a       |                                       |   |
| irrational.                                     | decimal expansion which repeats eventually    |                                       |   |
|   | into a rational number by analyzing repeating |                                       |   |
|   | patterns.                                     |                                       |   |

| Algebra I Standard                             | Previous Grade(s) Standards                  | Algebra I Standards Taught in Advance | Algebra I Standards Taught Concurrently          |
|--|--|---------------------------------------|--|
| A1: N-Q.A.1                                    | 6.RP.A.3                                     |                                       | A1: N-Q.A.2                                      |
| Use units as a way to understand problems      | Use ratio and rate reasoning to solve real-  |                                       | Define appropriate quantities for the purpose of |
| and to guide the solution of multi-step        | world and mathematical problems, e.g., by    |                                       | descriptive modeling.                            |
| problems; choose and interpret units           | reasoning about tables of equivalent ratios, |                                       |  |
| consistently in formulas; choose and interpret | tape diagrams, double number line diagrams,  |                                       |  |
| the scale and the origin in graphs and data    | or equations.                                |                                       |  |
| displays.                                      | a. Make tables of equivalent ratios relating |                                       |  |
|  | quantities with whole-number                 |                                       |  |
|  | measurements, find missing values in the     |                                       |  |
|  | tables, and plot the pairs of values on      |                                       |  |
|  | the coordinate plane. Use tables to          |                                       |  |
|  | compare ratios.                              |                                       |  |
|  | b. Solve unit rate problems including those  |                                       |  |
|  | involving unit pricing and constant          |                                       |  |
|  | speed. For example, if it took 7 hours to    |                                       |  |
|  | mow 4 lawns, then at that rate, now          |                                       |  |
|  | hours? At what unit rate were lawns          |                                       |  |
|  | hours: At what unit rate were lawis          |                                       |  |
|  | c Find a percent of a quantity as a rate per |                                       |  |
|  | 100  (e.g. 30% of a quantity means           |                                       |  |
|  | 30/100 times the quantity): solve            |                                       |  |
|  | problems involving finding the whole.        |                                       |  |
|  | given a part and the percent.                |                                       |  |
|  | d. Use ratio reasoning to convert            |                                       |  |
|  | measurement units; manipulate and            |                                       |  |
|  | transform units appropriately when           |                                       |  |
|  | multiplying or dividing quantities.          |                                       |  |
| A1: N-Q.A.2                                    |  |                                       | A1: N-Q.A.1                                      |
| Define appropriate quantities for the purpose  |  |                                       | Use units as a way to understand problems and    |
| of descriptive modeling.                       |  |                                       | to guide the solution of multi-step problems;    |
|  |  |                                       | choose and interpret units consistently in       |
|  |  |                                       | formulas; choose and interpret the scale and the |
|  |  |                                       | origin in graphs and data displays.              |
| A1: N-Q.A.3                                    | 8.EE.A.4                                     |                                       |  |
| Choose a level of accuracy appropriate to      | Perform operations with numbers expressed    |                                       |  |
| limitations on measurement when reporting      | in scientific notation, including problems   |                                       |  |
| quantities.                                    | where both decimal and scientific notation   |                                       |  |
|  | are used. Use scientific notation and choose |                                       |  |
|  | very large or very small quantities (o g use |                                       |  |
|  | millimotors per year for coeffeer encoding   |                                       |  |
|  | Interpret scientific notation that has been  |                                       |  |
|  | generated by technology                      |                                       |  |
|  | generated by technology.                     |                                       |  |

| Algebra I Standard   | Previous Grade(s) Standards   | Algebra I Standards Taught in Advance | Algebra I Standards Taught Concurrently |
|--|---|---------------------------------------|---|
| A1: A-SSE.A.1  | 6.EE.A.2  |                                       |   |
| <ul> <li>A1: A-SSE.A.1</li> <li>Interpret expressions that represent a quantity in terms of its context.</li> <li>a. Interpret parts of an expression, such as terms, factors, and coefficients.</li> <li>b. Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret P(1+r)<sup>n</sup> as the product of P and a factor not depending on P.</li> </ul> | <ul> <li><b>6.EE.A.2</b></li> <li>Write, read, and evaluate expressions in which letters stand for numbers.</li> <li>a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation "Subtract y from 5" as 5 - y.</li> <li>b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression 2 (8 + 7) as a product of two factors; view (8 + 7) as both a single entity and a sum of two terms.</li> <li>c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole-number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas V = s<sup>3</sup> and A = 6 s<sup>2</sup> to find the volume and surface area of a cube with sides of length s = 1/2.</li> <li><b>7.EE.A.2</b></li> <li>Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related. For example, a + 0.05a = 1.05a means that "increase by 5%" is the</li> </ul> |                                       |   |

| Algebra I Standard  | Previous Grade(s) Standards   | Algebra I Standards Taught in Advance  | Algebra I Standards Taught Concurrently   |
|---|---|--|---|
| A1: A-SSE.A.2<br>Use the structure of an expression to identify<br>ways to rewrite it. For example, see $x^4 - y^4$ as<br>$(x^2)^2 - (y^2)^2$ , or see $2x^2 + 8x$ as $(2x)(x) + 2x(4)$ ,<br>thus recognizing it as a polynomial whose<br>terms are products of monomials and the<br>polynomial can be factored as $2x(x+4)$ .  | <b>6.EE.A.3</b><br>Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression $3 (2 + x)$ to produce the equivalent expression $6 + 3x$ ; apply the distributive property to the expression $24x + 18y$ to produce the equivalent expression $6 (4x + 3y)$ ; apply properties of operations to $y + y + y$ to produce the equivalent expression $3y$ .<br><b>7.EE.A.1</b><br>Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients to include multiple grouping symbols (e.g., parentheses, brackets, and braces).   | <ul> <li>A1: A-SSE.A.1<br/>Interpret expressions that represent a quantity in terms of its context.</li> <li>a. Interpret parts of an expression, such as terms, factors, and coefficients.</li> <li>b. Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret P(1+r)<sup>n</sup> as the product of P and a factor not depending on P.</li> </ul>  |   |
| A1: A-SSE.B.3<br>Choose and produce an equivalent form of an<br>expression to reveal and explain properties of<br>the quantity represented by the expression.<br>a. Factor a quadratic expression to reveal<br>the zeros of the function it defines.<br>b. Complete the square in a quadratic<br>expression to reveal the maximum or<br>minimum value of the function it<br>defines.<br>c. Use the properties of exponents to<br>transform expressions for exponential<br>functions emphasizing integer<br>exponents. For example, the growth of<br>bacteria can be modeled by either $f(t) =$<br>$3^{(t+2)}$ or $g(t) = 9(3^t)$ because the<br>expression $3^{(t+2)}$ can be rewritten as<br>$(3^t)(3^2) = 9(3^t)$ . | <b>6.EE.A.3</b><br>Apply the properties of operations to<br>generate equivalent expressions. For<br>example, apply the distributive property to<br>the expression $3 (2 + x)$ to produce the<br>equivalent expression $6 + 3x$ ; apply the<br>distributive property to the expression $24x + 18y$ to produce the equivalent expression $6 (4x + 3y)$ ; apply properties of operations to $y + y + y$<br>y to produce the equivalent expression $3y$ .<br><b>7.EE.A.1</b><br>Apply properties of operations as strategies<br>to add, subtract, factor, and expand linear<br>expressions with rational coefficients to<br>include multiple grouping symbols (e.g.,<br>parentheses, brackets, and braces).<br><b>8.EE.A.1</b><br>Know and apply the properties of integer<br>exponents to generate equivalent numerical<br>expressions. For example, $3^2 \times 3^{-5} = 3^{-3} = 1/3^3 = 1/27$ . | <ul> <li>A1: A-SSE.A.1</li> <li>Interpret expressions that represent a quantity in terms of its context.</li> <li>a. Interpret parts of an expression, such as terms, factors, and coefficients.</li> <li>b. Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret P(1+r)<sup>n</sup> as the product of P and a factor not depending on P.</li> <li>A1: A-SSE.A.2</li> <li>Use the structure of an expression to identify ways to rewrite it. For example, see x<sup>4</sup> - y<sup>4</sup> as (x<sup>2</sup>)<sup>2</sup> - (y<sup>2</sup>)<sup>2</sup>, or see 2x<sup>2</sup> + 8x as (2x)(x) + 2x(4), thus recognizing it as a polynomial whose terms are products of monomials and the polynomial can be factored as 2x(x+4).</li> </ul> | <ul> <li>A1: A-RELB.4</li> <li>Solve quadratic equations in one variable.</li> <li>a. Use the method of completing the square to transform any quadratic equation in <i>x</i> into an equation of the form (<i>x</i> - <i>p</i>)<sup>2</sup> = <i>q</i> that has the same solutions. Derive the quadratic formula from this form.</li> <li>b. Solve quadratic equations by inspection (e.g., for <i>x</i><sup>2</sup> = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as "no real solution."</li> </ul> |

| Algebra I Standard   | Previous Grade(s) Standards  | Algebra I Standards Taught in Advance | Algebra I Standards Taught Concurrently |
|--|--|---------------------------------------|---|
| 1: A-APR.A.1<br>nderstand that polynomials form a system<br>nalogous to the integers, namely, they are<br>osed under the operations of addition,<br>ubtraction, and multiplication; add, subtract,<br>nd multiply polynomials. | <b>6.EE.A.3</b><br>Apply the properties of operations to<br>generate equivalent expressions. For<br>example, apply the distributive property to<br>the expression 3 (2 + x) to produce the<br>equivalent expression 6 + 3x; apply the<br>distributive property to the expression 24x +<br>18y to produce the equivalent expression 6 (4x<br>+ 3y); apply properties of operations to y + y +<br>y to produce the equivalent expression 3y.<br><b>6.EE.A.4</b><br>Identify when two expressions are equivalent<br>(i.e., when the two expressions name the<br>same number regardless of which value is<br>substituted into them). For example, the<br>expressions y + y + y and 3y are equivalent<br>because they name the same number<br>regardless of which number y stands for.<br><b>7.EE.A.1</b><br>Apply properties of operations as strategies<br>to add, subtract, factor, and expand linear<br>expressions with rational coefficients to<br>include multiple grouping symbols (e.g.,<br>parentheses, brackets, and braces).<br><b>8.EE.A.1</b><br>Know and apply the properties of integer<br>exponents to generate equivalent numerical<br>expressions. For example, $3^2 \times 3^{-5} = 3^{-3} =$<br>$1/3^3 = 1/27$ . |                                       |   |

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| Algebra I Standard   | Previous Grade(s) Standards   | Algebra I Standards Taught in Advance   | Algebra I Standards Taught Concurrently |
|--|---|---|---|
| A1: A-APR.B.3<br>Identify zeros of quadratic functions, and use<br>the zeros to sketch a graph of the function<br>defined by the polynomial. | 7.EE.A.1<br>Apply properties of operations as strategies<br>to add, subtract, factor, and expand linear<br>expressions with rational coefficients to<br>include multiple grouping symbols (e.g.,<br>parentheses, brackets, and braces). | A1: A-SSE.A.2<br>Use the structure of an expression to identify<br>ways to rewrite it. For example, see $x^4 - y^4$ as<br>$(x^2)^2 - (y^2)^2$ , or see $2x^2 + 8x$ as $(2x)(x) + 2x(4)$ ,<br>thus recognizing it as a polynomial whose<br>terms are products of monomials and the<br>polynomial can be factored as $2x(x+4)$ .<br>A1: A-SSE.B.3<br>Choose and produce an equivalent form of an<br>expression to reveal and explain properties of<br>the quantity represented by the expression.<br>a. Factor a quadratic expression to reveal<br>the zeros of the function it defines.<br>b. Complete the square in a quadratic<br>expression to reveal the maximum or<br>minimum value of the function it<br>defines.<br>c. Use the properties of exponents to<br>transform expressions for exponential<br>functions emphasizing integer<br>exponents. For example, the growth of<br>bacteria can be modeled by either $f(t) =$<br>$3^{(t+2)}$ or $g(t) = 9(3^t)$ because the<br>expression $3^{(t+2)}$ can be rewritten as<br>$(3^t)(3^2) = 9(3^t)$ . |   |

Create equations and inequalities in one

variable and use them to solve problems.

Include equations arising from linear,

quadratic, and exponential functions.

A1: A-CED.A.1

Previous Grade(s) Standards

#### Algebra I Standards Taught in Advance

### Algebra I Standards Taught Concurrently A1: A-REI.A.1

Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

#### A1: A-REI.B.3

Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

# 7.EE.B.4 Use variables to represent quantities in a real-

world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.

- a. Solve word problems leading to equations of the form px + q = r and p(x + q) = r, where p, q, and r are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm. Its length is 6 cm. What is its width?
- b. Solve word problems leading to inequalities of the form px + q > r,  $px + q \ge r$ , px + q < r or  $px + q \le r$ , where p, q, and r are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem. For example: As a salesperson, you are paid \$50 per week plus \$3 per sale. This week you want your pay to be at least \$100. Write an inequality for the number of sales you need to make, and describe the solutions.

# 8.EE.C.7

Solve linear equations in one variable.

- a. Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form x = a, a = a, or a = b results (where a and b are different numbers).
- Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms.

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| Algebra I Standard  | Previous Grade(s) Standards  | Algebra I Standards Taught in Advance  | Algebra I Standards Taught Concurrently  |
|---|--|--|--|
| A1: A-CED.A.2   | 8.EE.C.8   | A1: A-CED.A.1  | A1: A-REI.D.10   |
| Algebra I Standard<br>A1: A-CED.A.2<br>Create equations in two or more variables to<br>represent relationships between quantities;<br>graph equations on coordinate axes with<br>labels and scales. | <ul> <li>Previous Grade(s) Standards</li> <li>8.EE.C.8</li> <li>Analyze and solve pairs of simultaneous linear equations.</li> <li>a. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</li> <li>b. Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, 3x + 2y = 5 and 3x + 2y = 6 have no solution because 3x + 2y cannot simultaneously be 5 and 6.</li> <li>c. Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair.</li> <li>8.F.A.3</li> <li>Interpret the equation y = mx + b as defining a linear function, whose graph is a straight line; categorize functions as linear or nonlinear when given equations, graphs, or tables. For example, the function A = s<sup>2</sup>giving the area of a square as a function of its side length is not linear because its graph contains the points (1, 1), (2, 4) and (3, 9), which are not on a straight line.</li> <li>8.F.B.4</li> <li>Construct a function to model a linear relationship between two quantities.</li> </ul> | Algebra I Standards Taught in Advance          A1: A-CED.A1         Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear, quadratic, and exponential functions. | Algebra I Standards Taught Concurrently A1: A-REI.D.10 Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line). |
|   | Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two $(x, y)$ values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.  |  |  |

| Algebra I Standard  | Previous Grade(s) Standards | Algebra I Standards Taught in Advance   | Algebra I Standards Taught Concurrently  |
|---|-----------------------------|---|--|
| A1: A-CED.A.3<br>Represent constraints by equations or<br>inequalities, and by systems of equations<br>and/or inequalities, and interpret solutions as<br>viable or nonviable options in a modeling<br>context. For example, represent inequalities<br>describing nutritional and cost constraints on<br>combinations of different foods. |                             | A1: A-CED.A.1<br>Create equations and inequalities in one<br>variable and use them to solve problems.<br>Include equations arising from linear,<br>quadratic, and exponential functions.<br>A1: A-CED.A.2<br>Create equations in two or more variables to<br>represent relationships between quantities;<br>graph equations on coordinate axes with<br>labels and scales.<br>A1: A-REI.D.10<br>Understand that the graph of an equation in<br>two variables is the set of all its solutions<br>plotted in the coordinate plane, often forming<br>a curve (which could be a line). |  |
| A1: A-CED.A.4<br>Rearrange formulas to highlight a quantity of<br>interest, using the same reasoning as in<br>solving equations. For example, rearrange<br>Ohm's law V = IR to highlight resistance R.  |                             | A1: A-CED.A.2<br>Create equations in two or more variables to<br>represent relationships between quantities;<br>graph equations on coordinate axes with<br>labels and scales.   | A1: A-REI.A.1<br>Explain each step in solving a simple equation as<br>following from the equality of numbers asserted<br>at the previous step, starting from the<br>assumption that the original equation has a<br>solution. Construct a viable argument to justify a<br>solution method.<br>A1: A-REI.B.3<br>Solve linear equations and inequalities in one<br>variable, including equations with coefficients<br>represented by letters. |

## A1: A-REI.A.1

Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

#### Previous Grade(s) Standards

# 7.EE.B.4

Use variables to represent quantities in a realworld or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.

- a. Solve word problems leading to equations of the form px + q = r and p(x + q) = r, where p, q, and r are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm. Its length is 6 cm. What is its width?
- b. Solve word problems leading to inequalities of the form px + q > r,  $px + q \ge r$ , px + q < r or  $px + q \le r$ , where p, q, and r are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem. For example: As a salesperson, you are paid \$50 per week plus \$3 per sale. This week you want your pay to be at least \$100. Write an inequality for the number of sales you need to make, and describe the solutions.

# 8.EE.C.7

Solve linear equations in one variable.

- a. Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form x = a, a = a, or a = b results (where a and b are different numbers).
- Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms.

#### Algebra I Standards Taught in Advance

### Algebra I Standards Taught Concurrently A1: A-CED.A.1

Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear, quadratic, and exponential functions.

#### A1: A-CED.A.4

Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law V = IR to highlight resistance R.

#### A1: A-REI.B.3

Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

#### A1: A-REI.B.4

Solve quadratic equations in one variable.

- a. Use the method of completing the square to transform any quadratic equation in x into an equation of the form  $(x - p)^2 = q$  that has the same solutions. Derive the quadratic formula from this form.
- b. Solve quadratic equations by inspection (e.g., for  $x^2 = 49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as "no real solution."

Solve linear equations and inequalities in one

variable, including equations with coefficients

A1: A-REI.B.3

represented by letters.

7.EE.B.4

Previous Grade(s) Standards

#### Algebra I Standards Taught in Advance

### Algebra I Standards Taught Concurrently A1: A-CED.A.1

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#### A1: A-CED.A.4

Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law V = IR to highlight resistance R.

#### A1: A-REI.A.1

Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

#### A1: A-REI.B.4

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- a. Use the method of completing the square to transform any quadratic equation in x into an equation of the form  $(x - p)^2 = q$  that has the same solutions. Derive the quadratic formula from this form.
- b. Solve quadratic equations by inspection (e.g., for  $x^2 = 49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as "no real solution."

Use variables to represent quantities in a realworld or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.

- a. Solve word problems leading to equations of the form px + q = r and p(x + q) = r, where p, q, and r are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm. Its length is 6 cm. What is its width?
- b. Solve word problems leading to inequalities of the form px + q > r,  $px + q \ge r$ , px + q < r or  $px + q \le r$ , where p, q, and r are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem. For example: As a salesperson, you are paid \$50 per week plus \$3 per sale. This week you want your pay to be at least \$100. Write an inequality for the number of sales you need to make, and describe the solutions.

# 8.EE.C.7

Solve linear equations in one variable.

- a. Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form x = a, a = a, or a = b results (where a and b are different numbers).
- Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms.

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## A1: A-REI.B.4

Solve quadratic equations in one variable.

- a. Use the method of completing the square to transform any quadratic equation in x into an equation of the form  $(x p)^2 = q$  that has the same solutions. Derive the quadratic formula from this form.
- b. Solve quadratic equations by inspection (e.g., for  $x^2 = 49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as "no real solution."

# Previous Grade(s) Standards

# 7.EE.A.1

Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients to include multiple grouping symbols (e.g., parentheses, brackets, and braces).

# 8.EE.A.2

Use square root and cube root symbols to represent solutions to equations of the form  $x^2 = p$  and  $x^3 = p$ , where p is a positive rational number. Evaluate square roots of small perfect squares and cube roots of small perfect cubes. Know that  $\sqrt{2}$  is irrational.

#### Algebra I Standards Taught in Advance

### Algebra I Standards Taught Concurrently A1: A-SSE.B.3

Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.

- a. Factor a quadratic expression to reveal the zeros of the function it defines.
- b. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines.
- c. Use the properties of exponents to transform expressions for exponential functions emphasizing integer exponents. For example, the growth of bacteria can be modeled by either  $f(t) = 3^{(t+2)}$  or  $g(t) = 9(3^t)$  because the expression  $3^{(t+2)}$  can be rewritten as  $(3^t)(3^2) = 9(3^t)$ .

#### A1: A-CED.A.1

Create equations and inequalities in one variable and use them to solve problems. *Include equations arising from linear, quadratic, and exponential functions.* 

### A1: A-REI.A.1

Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

### A1: A-REI.B.3

Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

| Algebra I Standard  | Previous Grade(s) Standards   | Algebra I Standards Taught in Advance | Algebra I Standards Taught Concurrently   |
|---|---|---------------------------------------|---|
| A1: A-REI.C.5<br>Prove that, given a system of two equations in   | 8.EE.C.8<br>Analyze and solve pairs of simultaneous linear  |                                       | A1: A-REI.C.6<br>Solve systems of linear equations exactly and  |
| Prove that, given a system of two equations in<br>two variables, replacing one equation by the<br>sum of that equation and a multiple of the<br>other produces a system with the same<br>solutions. | <ul> <li>Analyze and solve pairs of simultaneous linear equations.</li> <li>a. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</li> <li>b. Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, 3x + 2y = 5 and 3x + 2y = 6 have no solution because 3x + 2y cannot simultaneously be 5 and 6.</li> <li>c. Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of points, detarming whather the line through the</li> </ul>  |                                       | solve systems of linear equations exactly and<br>approximately (e.g., with graphs), focusing on<br>pairs of linear equations in two variables.  |
|   | determine whether the line through the<br>first pair of points intersects the line<br>through the second pair.  |                                       |   |
| A1: A-REI.C.6<br>Solve systems of linear equations exactly and<br>approximately (e.g., with graphs), focusing on<br>pairs of linear equations in two variables.                                     | <ul> <li>8.EE.C.8</li> <li>Analyze and solve pairs of simultaneous linear equations.</li> <li>a. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</li> <li>b. Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, 3x + 2y = 5 and 3x + 2y = 6 have no solution because 3x + 2y cannot simultaneously be 5 and 6.</li> <li>c. Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line</li> </ul> |                                       | A1: A-REI.C.5<br>Prove that, given a system of two equations in<br>two variables, replacing one equation by the<br>sum of that equation and a multiple of the other<br>produces a system with the same solutions. |

| Algebra I Standard  | Previous Grade(s) Standards  | Algebra I Standards Taught in Advance   | Algebra I Standards Taught Concurrently   |
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| A1: A-REI.D.10<br>Understand that the graph of an equation in<br>two variables is the set of all its solutions<br>plotted in the coordinate plane, often forming<br>a curve (which could be a line).  | 8.EE.B.5<br>Graph proportional relationships, interpreting<br>the unit rate as the slope of the graph.<br>Compare two different proportional<br>relationships represented in different ways.<br>For example, compare a distance-time graph<br>to a distance-time equation to determine<br>which of two moving objects has greater<br>speed.  |   | A1: A-CED.A.2<br>Create equations in two or more variables to<br>represent relationships between quantities;<br>graph equations on coordinate axes with labels<br>and scales. |
| A1: A-REI.D.11<br>Explain why the x-coordinates of the points<br>where the graphs of the equations $y = f(x)$<br>and $y = g(x)$ intersect are the solutions of the<br>equation $f(x) = g(x)$ ; find the solutions<br>approximately, e.g., using technology to<br>graph the functions, make tables of values, or<br>find successive approximations. Include cases<br>where $f(x)$ and/or $g(x)$ are linear, polynomial,<br>rational, piecewise linear (to include absolute<br>value), and exponential functions. | <ul> <li>8. FE.C.8<br/>Analyze and solve pairs of simultaneous linear equations.</li> <li>a. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</li> <li>b. Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, 3x + 2y = 5 and 3x + 2y = 6 have no solution because 3x + 2y cannot simultaneously be 5 and 6.</li> <li>c. Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair.</li> </ul> | A1: A-REI.C.6<br>Solve systems of linear equations exactly and<br>approximately (e.g., with graphs), focusing on<br>pairs of linear equations in two variables.<br>A1: A-REI.D.10<br>Understand that the graph of an equation in<br>two variables is the set of all its solutions<br>plotted in the coordinate plane, often forming<br>a curve (which could be a line). |   |
| A1: A-REI.D.12<br>Graph the solutions to a linear inequality in<br>two variables as a half-plane (excluding the<br>boundary in the case of a strict inequality),<br>and graph the solution set to a system of<br>linear inequalities in two variables as the<br>intersection of the corresponding half-planes.  |  | A1: A-REI.C.6<br>Solve systems of linear equations exactly and<br>approximately (e.g., with graphs), focusing on<br>pairs of linear equations in two variables.<br>A1: A-REI.D.10<br>Understand that the graph of an equation in<br>two variables is the set of all its solutions<br>plotted in the coordinate plane, often forming<br>a curve (which could be a line). |   |

| Algebra I Standard   | Previous Grade(s) Standards                                 | Algebra I Standards Taught in Advance | Algebra I Standards Taught Concurrently |
|--|---|---------------------------------------|---|
| 1: F-IF.A.1  | 8.F.A.1   |                                       |   |
| Understand that a function from one set                        | Understand that a function is a rule that                   |                                       |   |
| called the domain) to another set (called the                  | assigns to each input exactly one output. The               |                                       |   |
| range) assigns to each element of the domain                   | graph of a function is the set of ordered pairs             |                                       |   |
| exactly one element of the range. If <i>f</i> is a             | consisting of an input and the corresponding                |                                       |   |
| function and x is an element of its domain,                    | output. (Function notation is not required in               |                                       |   |
| then $f(x)$ denotes the output of $f$                          | this grade level.)  |                                       |   |
| corresponding to the input <i>x</i> . The graph of <i>f</i> is | 8.F.A.2   |                                       |   |
| the graph of the equation $y = f(x)$ .                         | Compare properties of two functions each                    |                                       |   |
|  | represented in a different way (algebraically,              |                                       |   |
|  | graphically, numerically in tables, or by verbal            |                                       |   |
|  | descriptions). For example, given a linear                  |                                       |   |
|  | function represented by a table of values and               |                                       |   |
|  | a linear function represented by an algebraic               |                                       |   |
|  | expression, determine which function has the                |                                       |   |
|  | greater rate of change.                                     |                                       |   |
|  | 8.F.A.3   |                                       |   |
|  | Interpret the equation y = mx + b as defining a             |                                       |   |
|  | linear function, whose graph is a straight line;            |                                       |   |
|  | categorize functions as linear or nonlinear                 |                                       |   |
|  | when given equations, graphs, or tables. For                |                                       |   |
|  | example, the function A = s <sup>2</sup> giving the area of |                                       |   |
|  | a square as a function of its side length is not            |                                       |   |
|  | linear because its graph contains the points                |                                       |   |
|  | (1, 1), (2, 4) and (3, 9), which are not on a               |                                       |   |
|  | straight line.  |                                       |   |

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|--|---|--|--|
| Algebra I Standard<br>A1: F-IF.A.2<br>Use function notation, evaluate functions for<br>inputs in their domains, and interpret<br>statements that use function notation in<br>terms of a context.               | <ul> <li>6.EE.A.2</li> <li>Write, read, and evaluate expressions in which letters stand for numbers.</li> <li>a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation "Subtract y from 5" as 5 - y.</li> <li>b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression 2 (8 + 7) as a product of two factors; view (8 + 7) as both a single entity and a sum of two terms.</li> <li>c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole-number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas V = s<sup>3</sup> and A = 6 s<sup>2</sup> to find the volume and surface area of a cube with sides of length s = 1/2</li> </ul> | Algebra 1 Standards Taught in Advance<br>A1: F-IF.A.1<br>Understand that a function from one set<br>(called the domain) to another set (called the<br>range) assigns to each element of the domain<br>exactly one element of the range. If $f$ is a<br>function and $x$ is an element of its domain,<br>then $f(x)$ denotes the output of $f$<br>corresponding to the input $x$ . The graph of $f$ is<br>the graph of the equation $y = f(x)$ .  | Algebra I Standards Taught Concurrently  |
| A1: F-IF.A.3<br>Recognize that sequences are functions<br>whose domain is a subset of the<br>integers. Relate arithmetic sequences to<br>linear functions and geometric sequences to<br>exponential functions. |   | A1: F-IF.A.1<br>Understand that a function from one set<br>(called the domain) to another set (called the<br>range) assigns to each element of the domain<br>exactly one element of the range. If $f$ is a<br>function and $x$ is an element of its domain,<br>then $f(x)$ denotes the output of $f$<br>corresponding to the input $x$ . The graph of $f$ is<br>the graph of the equation $y = f(x)$ .<br>A1: F-IF.A.2<br>Use function notation, evaluate functions for<br>inputs in their domains, and interpret<br>statements that use function notation in<br>terms of a context. | <ul> <li>A1: F-BF.A.1</li> <li>Write a linear, quadratic, or exponential function that describes a relationship between two quantities.</li> <li>a. Determine an explicit expression, a recursive process, or steps for calculation from a context.</li> </ul> |

| Algebra I Standard                              | Previous Grade(s) Standards                     | Algebra I Standards Taught in Advance  | Algebra I Standards Taught Concurrently |
|---|---|--|---|
| A1: F-IF.B.4                                    | 8.F.B.5   | A1: F-IF.A.1   |   |
| For linear, piecewise linear (to include        | Describe qualitatively the functional           | Understand that a function from one set  |   |
| absolute value), quadratic, and exponential     | relationship between two quantities by          | (called the domain) to another set (called the   |   |
| functions that model a relationship between     | analyzing a graph (e.g., where the function is  | range) assigns to each element of the domain   |   |
| two quantities, interpret key features of       | increasing or decreasing, linear or nonlinear). | exactly one element of the range. If <i>f</i> is a                                     |   |
| graphs and tables in terms of the quantities,   | Sketch a graph that exhibits the qualitative    | function and x is an element of its domain,  |   |
| and sketch graphs showing key features given    | features of a function that has been described  | then $f(x)$ denotes the output of $f$  |   |
| a verbal description of the relationship. Key   | verbally.                                       | corresponding to the input <i>x</i> . The graph of <i>f</i> is                         |   |
| features include: intercepts; intervals where   |   | the graph of the equation $y = f(x)$ .   |   |
| the function is increasing, decreasing,         |   | A1: N-Q.A.1  |   |
| positive, or negative; relative maximums and    |   | Use units as a way to understand problems  |   |
| minimums; symmetries; and end behavior.         |   | and to guide the solution of multi-step  |   |
|   |   | problems; choose and interpret units   |   |
|   |   | consistently in formulas; choose and interpret   |   |
|   |   | the scale and the origin in graphs and data  |   |
|   |   | displays.  |   |
| A1: F-IF.B.5                                    |   | A1: F-IF.A.1   |   |
| Relate the domain of a function to its graph    |   | Understand that a function from one set  |   |
| and, where applicable, to the quantitative      |   | (called the domain) to another set (called the   |   |
| relationship it describes. For example, if the  |   | range) assigns to each element of the domain   |   |
| function h(n) gives the number of person-       |   | exactly one element of the range. If f is a  |   |
| hours it takes to assemble n engines in a       |   | function and x is an element of its domain,  |   |
| factory, then the positive integers would be an |   | then $f(x)$ denotes the output of $f$  |   |
| appropriate domain for the function.            |   | corresponding to the input x. The graph of f is  |   |
|   |   | the graph of the equation $y = f(x)$ .   |   |
|   |   |  |   |
|   |   | For linear, piecewise linear (to include   |   |
|   |   | absolute value), quadratic, and exponential  |   |
|   |   | functions that model a relationship between  |   |
|   |   | two quantities, interpret key features of  |   |
|   |   | graphs and tables in terms of the quantities,  |   |
|   |   | and sketch graphs showing key features given   |   |
|   |   | a verbal description of the relationship. Key  |   |
|   |   | the function is increasing decreasing  |   |
|   |   | ne junction is increasing, decreasing,   |   |
|   |   | positive, or negative; relative maximums and<br>minimums; symmetrics; and and behavior |   |
|   |   | minimums; symmetries; and end bendvlor.  |   |

| Algebra I Standard  | Previous Grade(s) Standards  | Algebra I Standards Taught in Advance   | Algebra I Standards Taught Concurrently   |
|---|--|---|---|
| A1: F-IF.B.6<br>Calculate and interpret the average rate of<br>change of a linear, quadratic, piecewise linear<br>(to include absolute value), and exponential<br>function (presented symbolically or as a table)<br>over a specified interval. Estimate the rate of<br>change from a graph.  | <b>8.F.B.4</b><br>Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two $(x, y)$ values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph  | A1: F-IF.A.2<br>Use function notation, evaluate functions for<br>inputs in their domains, and interpret<br>statements that use function notation in<br>terms of a context.  |   |
| <ul> <li>A1: F-IF.C.7</li> <li>Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.</li> <li>a. Graph linear and quadratic functions and show intercepts, maxima, and minima.</li> <li>b. Graph piecewise linear (to include absolute value) and exponential functions.</li> </ul> | or a table of values.<br><b>8.EE.B.5</b><br>Graph proportional relationships, interpreting<br>the unit rate as the slope of the graph.<br>Compare two different proportional<br>relationships represented in different ways.<br>For example, compare a distance-time graph<br>to a distance-time equation to determine<br>which of two moving objects has greater<br>speed.<br><b>8.F.A.3</b><br>Interpret the equation $y = mx + b$ as defining a<br>linear function, whose graph is a straight line;<br>categorize functions as linear or nonlinear<br>when given equations, graphs, or tables. For<br>example, the function $A = s^2giving$ the area of<br>a square as a function of its side length is not<br>linear because its graph contains the points<br>(1, 1), (2, 4) and (3, 9), which are not on a<br>straight line | A1: F-IF.A.1<br>Understand that a function from one set<br>(called the domain) to another set (called the<br>range) assigns to each element of the domain<br>exactly one element of the range. If <i>f</i> is a<br>function and <i>x</i> is an element of its domain,<br>then $f(x)$ denotes the output of <i>f</i><br>corresponding to the input <i>x</i> . The graph of <i>f</i> is<br>the graph of the equation $y = f(x)$ . | A1: F-IF.C.8<br>Write a function defined by an expression in<br>different but equivalent forms to reveal and<br>explain different properties of the function.<br>Use the process of factoring and completing the<br>square in a quadratic function to show zeros,<br>extreme values, and symmetry of the graph, and<br>interpret these in terms of a context.<br>A1: F-BF.B.3<br>Identify the effect on the graph of replacing $f(x)$<br>by $f(x) + k$ , $k f(x)$ , $f(kx)$ , and $f(x + k)$ for specific<br>values of $k$ (both positive and negative). Without<br>technology, find the value of $k$ given the graphs<br>of linear and quadratic functions. With<br>technology, experiment with cases and illustrate<br>an explanation of the effects on the graph that<br>include cases where $f(x)$ is a linear, quadratic,<br>piecewise linear (to include absolute value) or<br>exponential function |
| <ul> <li>A1: F-IF.C.8</li> <li>Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.</li> <li>a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.</li> </ul> | <b>7.EE.A.1</b><br>Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients to include multiple grouping symbols (e.g., parentheses, brackets, and braces).   |   | <ul> <li>A1: F-IF.C.7</li> <li>Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.</li> <li>a. Graph linear and quadratic functions and show intercepts, maxima, and minima.</li> <li>b. Graph piecewise linear (to include absolute value) and exponential functions.</li> </ul>   |

| Algebra I Standard   | Previous Grade(s) Standards  | Algebra I Standards Taught in Advance   | Algebra I Standards Taught Concurrently  |
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| A1: F-IF.C.9<br>Compare properties of two functions (linear,<br>quadratic, piecewise linear [to include<br>absolute value] or exponential) each<br>represented in a different way (algebraically,<br>graphically, numerically in tables, or by verbal<br>descriptions). For example, given a graph of<br>one quadratic function and an algebraic<br>expression for another, determine which has<br>the larger maximum.   |  | A1: F-IF.B.4<br>For linear, piecewise linear (to include<br>absolute value), quadratic, and exponential<br>functions that model a relationship between<br>two quantities, interpret key features of<br>graphs and tables in terms of the quantities,<br>and sketch graphs showing key features given<br>a verbal description of the relationship. <i>Key</i><br><i>features include: intercepts; intervals where</i><br><i>the function is increasing, decreasing,</i><br><i>positive, or negative; relative maximums and</i><br><i>minimums; symmetries; and end behavior.</i><br>A1: F-IF.C.8<br>Write a function defined by an expression in<br>different but equivalent forms to reveal and<br>explain different properties of the function.<br>Use the process of factoring and completing<br>the square in a quadratic function to show<br>zeros, extreme values, and symmetry of the<br>graph, and interpret these in terms of a<br>context. |  |
| <ul> <li>A1: F-BF.A.1</li> <li>Write a linear, quadratic, or exponential function that describes a relationship between two quantities.</li> <li>a. Determine an explicit expression, a recursive process, or steps for calculation from a context.</li> </ul>   | <b>8.F.B.4</b><br>Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two ( <i>x</i> , <i>y</i> ) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values. |   | A1: F-IF.A.3<br>Recognize that sequences are functions whose<br>domain is a subset of the integers. Relate<br>arithmetic sequences to linear functions and<br>geometric sequences to exponential functions.  |
| A1: F-BF.B.3<br>Identify the effect on the graph of<br>replacing $f(x)$ by $f(x) + k$ , $k f(x)$ , $f(kx)$ ,<br>and $f(x + k)$ for specific values of $k$ (both<br>positive and negative). Without technology,<br>find the value of $k$ given the graphs of linear<br>and quadratic functions. With technology,<br>experiment with cases and illustrate an<br>explanation of the effects on the graph that<br>include cases where $f(x)$ is a linear, quadratic,<br>piecewise linear (to include absolute value) or<br>exponential function. |  |   | <ul> <li>A1: F-IF.C.7<br/>Graph functions expressed symbolically and<br/>show key features of the graph, by hand in<br/>simple cases and using technology for more<br/>complicated cases.</li> <li>a. Graph linear and quadratic functions and<br/>show intercepts, maxima, and minima.</li> <li>b. Graph piecewise linear (to include absolute<br/>value) and exponential functions.</li> </ul> |

| Algebra I Standard  | Previous Grade(s) Standards   | Algebra I Standards Taught in Advance   | Algebra I Standards Taught Concurrently |
|---|---|---|---|
| <ul> <li>A1: F-LE.A.1</li> <li>Distinguish between situations that can be modeled with linear functions and with exponential functions.</li> <li>a. Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.</li> <li>b. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.</li> <li>c. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.</li> </ul> | <b>8.F.A.3</b><br>Interpret the equation $y = mx + b$ as defining a linear function, whose graph is a straight line; categorize functions as linear or nonlinear when given equations, graphs, or tables. For example, the function $A = s^2 giving$ the area of a square as a function of its side length is not linear because its graph contains the points (1, 1), (2, 4) and (3, 9), which are not on a straight line.<br><b>8.F.B.4</b><br>Construct a function to model a linear relationship between two quantities.<br>Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values. |   |   |
| A1: F-LE.A.2<br>Construct linear and exponential functions,<br>including arithmetic and geometric<br>sequences, given a graph, a description of a<br>relationship, or two input-output pairs<br>(include reading these from a table).   | <b>8.F.B.4</b><br>Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two ( <i>x</i> , <i>y</i> ) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.  | <ul> <li>A1: F-LE.A.1</li> <li>Distinguish between situations that can be modeled with linear functions and with exponential functions.</li> <li>a. Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.</li> <li>b. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.</li> <li>c. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.</li> </ul> |   |

| Algebra I Standard                           | Previous Grade(s) Standards | Algebra I Standards Taught in Advance  | Algebra I Standards Taught Concurrently |
|--|-----------------------------|--|---|
| A1: F-LE.A.3                                 |                             | A1: F-LE.A.1   |   |
| Observe using graphs and tables that a       |                             | Distinguish between situations that can be   |   |
| quantity increasing exponentially eventually |                             | modeled with linear functions and with   |   |
| exceeds a quantity increasing linearly,      |                             | exponential functions.   |   |
| quadratically, or (more generally) as a      |                             | a. Prove that linear functions grow by equal   |   |
| polynomial function.                         |                             | differences over equal intervals, and that   |   |
|  |                             | exponential functions grow by equal  |   |
|  |                             | factors over equal intervals.  |   |
|  |                             | b. Recognize situations in which one   |   |
|  |                             | quantity changes at a constant rate per  |   |
|  |                             | unit interval relative to another.   |   |
|  |                             | c. Recognize situations in which a quantity  |   |
|  |                             | grows or decays by a constant percent  |   |
|  |                             | rate per unit interval relative to another.  |   |
| A1: F-LE.B.5                                 |                             | A1: F-BF.B.3   |   |
| Interpret the parameters in a linear or      |                             | Identify the effect on the graph of  |   |
| exponential function in terms of a context.  |                             | replacing $f(x)$ by $f(x) + k$ , $k f(x)$ , $f(kx)$ ,  |   |
|  |                             | and $f(x + k)$ for specific values of k (both  |   |
|  |                             | positive and negative). Without technology,  |   |
|  |                             | find the value of k given the graphs of linear   |   |
|  |                             | and quadratic functions. With technology,  |   |
|  |                             | experiment with cases and illustrate an  |   |
|  |                             | explanation of the effects on the graph that   |   |
|  |                             | include cases where $f(x)$ is a linear, quadratic,   |   |
|  |                             | piecewise linear (to include absolute value) or  |   |
|  |                             |  |   |
|  |                             | AI. F-LE.A.Z   |   |
|  |                             | including arithmetic and geometric   |   |
|  |                             | sequences given a graph a description of a   |   |
|  |                             | relationshin or two input-output nairs   |   |
|  |                             | (include reading these from a table)   |   |
|  |                             | sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table). |   |

| Algebra I Standard   | Previous Grade(s) Standards  | Algebra I Standards Taught in Advance | Algebra I Standards Taught Concurrently   |
|--|--|---------------------------------------|---|
| A1: S-ID.A.2<br>Use statistics appropriate to the shape of the<br>data distribution to compare center (median,<br>mean) and spread (interquartile range,<br>standard deviation) of two or more different<br>data sets. | <ul> <li>6.SP.A.2</li> <li>Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.</li> <li>6.SP.B.5</li> <li>Summarize numerical data sets in relation to their context, such as by: <ul> <li>a. Reporting the number of observations.</li> <li>b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> </ul> </li> <li>C. Giving quantitative measures of center (median and/or mean) and variability (interquartile range), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</li> <li>d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were described as the late.</li> </ul> |                                       | A1: S-ID.A.3<br>Interpret differences in shape, center, and<br>spread in the context of the data sets,<br>accounting for possible effects of extreme data<br>points (outliers).                                     |
| A1: S-ID.A.3<br>Interpret differences in shape, center, and<br>spread in the context of the data sets,<br>accounting for possible effects of extreme<br>data points (outliers).  | <ul> <li>6.SP.B.5</li> <li>Summarize numerical data sets in relation to their context, such as by: <ul> <li>a. Reporting the number of observations.</li> <li>b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> </ul> </li> <li>c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</li> <li>d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.</li> </ul>  |                                       | A1: S-ID.A.2<br>Use statistics appropriate to the shape of the<br>data distribution to compare center (median,<br>mean) and spread (interquartile range, standard<br>deviation) of two or more different data sets. |

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| A1: S-ID.B.5                                     | 8.SP.A.4  |                                       |   |
| Summarize categorical data for two               | Understand that patterns of association can     |                                       |   |
| categories in two-way frequency tables.          | also be seen in bivariate categorical data by   |                                       |   |
| Interpret relative frequencies in the context    | displaying frequencies and relative             |                                       |   |
| of the data (including joint, marginal, and      | frequencies in a two-way table. Construct and   |                                       |   |
| conditional relative frequencies). Recognize     | interpret a two-way table summarizing data      |                                       |   |
| possible associations and trends in the data.    | on two categorical variables collected from     |                                       |   |
|  | the same subjects. Use relative frequencies     |                                       |   |
|  | calculated for rows or columns to describe      |                                       |   |
|  | possible association between the two            |                                       |   |
|  | variables. For example, collect data from       |                                       |   |
|  | students in your class on whether or not they   |                                       |   |
|  | have a curfew on school nights and whether      |                                       |   |
|  | or not they have assigned chores at home. Is    |                                       |   |
|  | there evidence that those who have a curfew     |                                       |   |
|  | also tend to have chores?                       |                                       |   |
| A1: S-ID.B.6                                     | 8.SP.A.1  |                                       |   |
| Represent data on two quantitative variables     | Construct and interpret scatter plots for       |                                       |   |
| on a scatter plot, and describe how the          | bivariate measurement data to investigate       |                                       |   |
| variables are related.                           | patterns of association between two             |                                       |   |
| a. Fit a function to the data; use functions     | quantities. Describe patterns such as           |                                       |   |
| fitted to data to solve problems in the          | clustering, outliers, positive or negative      |                                       |   |
| context of the data. Use given functions         | association, linear association, and nonlinear  |                                       |   |
| or choose a function suggested by the            | association.                                    |                                       |   |
| context. Emphasize linear and quadratic          | 8.SP.A.2  |                                       |   |
| models.  | Know that straight lines are widely used to     |                                       |   |
| b. Informally assess the fit of a function by    | model relationships between two                 |                                       |   |
| plotting and analyzing residuals.                | quantitative variables. For scatter plots that  |                                       |   |
| c. Fit a linear function for a scatter plot that | suggest a linear association, informally fit a  |                                       |   |
| suggests a linear association.                   | straight line, and informally assess the model  |                                       |   |
|  | fit by judging the closeness of the data points |                                       |   |
|  | to the line.                                    |                                       |   |
|  | 8.SP.A.3  |                                       |   |
|  | Use the equation of a linear model to solve     |                                       |   |
|  | problems in the context of bivariate            |                                       |   |
|  | measurement data, interpreting the slope        |                                       |   |
|  | and intercept. For example, in a linear model   |                                       |   |
|  | for a biology experiment, interpret a slope of  |                                       |   |
|  | 1.5 cm/hr as meaning that an additional hour    |                                       |   |
|  | of sunlight each day is associated with an      |                                       |   |
|  | additional 1.5 cm in mature plant height.       |                                       |   |

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| A1: S-ID.C.7<br>Interpret the slope (rate of change) and the<br>intercept (constant term) of a linear model in<br>the context of the data. | <b>8.SP.A.3</b><br>Use the equation of a linear model to solve<br>problems in the context of bivariate<br>measurement data, interpreting the slope<br>and intercept. For example, in a linear model<br>for a biology experiment, interpret a slope of<br>1.5 cm/hr as meaning that an additional hour<br>of sunlight each day is associated with an<br>additional 1.5 cm in mature plant height. | <ul> <li>A1: S-ID.B.6</li> <li>Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.</li> <li>a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear and quadratic models.</li> <li>b. Informally assess the fit of a function by plotting and analyzing residuals.</li> <li>c. Fit a linear function for a scatter plot that suggests a linear association.</li> </ul>                                |  |
| A1: S-ID.C.8<br>Compute (using technology) and interpret the<br>correlation coefficient of a linear fit.                                   |  | <ul> <li>A1: S-ID.B.6<br/>Represent data on two quantitative variables<br/>on a scatter plot, and describe how the<br/>variables are related.</li> <li>a. Fit a function to the data; use functions<br/>fitted to data to solve problems in the<br/>context of the data. Use given functions<br/>or choose a function suggested by the<br/>context. Emphasize linear and quadratic<br/>models.</li> <li>b. Informally assess the fit of a function by<br/>plotting and analyzing residuals.</li> <li>c. Fit a linear function for a scatter plot that<br/>suggests a linear association.</li> </ul> | A1: S-ID.C.9<br>Distinguish between correlation and causation.   |
| A1: S-ID.C.9<br>Distinguish between correlation and<br>causation.  |  | <ul> <li>A1: S-ID.B.6</li> <li>Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.</li> <li>a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear and quadratic models.</li> <li>b. Informally assess the fit of a function by plotting and analyzing residuals.</li> <li>c. Fit a linear function for a scatter plot that suggests a linear association.</li> </ul>                                | A1: S-ID.C.8<br>Compute (using technology) and interpret the<br>correlation coefficient of a linear fit. |